

1-1 解:  $\therefore \Delta y = y_{j+1} - y_j = \frac{r_0}{d} \lambda$

$$\therefore \Delta y_1 = \frac{180}{0.022} \times 5000 \times 10^{-8} \approx 0.409 \text{ cm}$$

$$\Delta y_2 = \frac{180}{0.022} \times 2000 \times 10^{-8} \approx 0.573 \text{ cm}$$

又:  $y = j \frac{r_0}{d} \lambda, \quad j = 2$

$$\therefore \Delta y = j \frac{r_0}{d} (\lambda_2 - \lambda_1) = 2 \times \frac{180}{0.022} \times (7000 - 5000) \times 10^{-8} \\ \approx 0.327 \text{ cm}$$

or:  $\Delta y = 2\Delta y_2 - 2\Delta y_1 \approx 0.328 \text{ cm}$

1-2 解:  $\therefore \left( \Delta y = \frac{r_0}{d} \lambda \right), \quad y = j \frac{r_0}{d} \lambda \quad j=0, 1$

$$\therefore (1) \quad \Delta y = (1-0) \times \frac{50}{0.04} \times 6.4 \times 10^{-5} = 0.08 \text{ cm}$$

(2)

$$\Delta \varphi = j \cdot 2\pi = 2\pi \cdot \frac{dy}{r_0 \lambda} = 2\pi \times \frac{0.04 \times 0.001}{50 \times 6.4 \times 10^{-5}} = \frac{\pi}{4}$$

$$I = 4A_1^2 \cos^2 \frac{\varphi_2 - \varphi_1}{2} \quad (3)$$

$$I_0 = 4A_1^2$$

$$\varphi_2 - \varphi_1 = \frac{\pi}{4}$$

$$\frac{I_p}{I_0} = \cos^2 \frac{\pi/4}{2} = \cos^2 \frac{\pi}{8} \approx 0.854$$

1-3 解:  $\therefore \delta = nd - d = (n-1)d \quad (\Delta \varphi = \frac{2\pi}{\lambda} \delta = j \cdot 2\pi)$

而:  $\delta = j\lambda$

$$\therefore d = \frac{j\lambda}{n-1} = \frac{5 \times 6 \times 10^{-7}}{1.5-1} = 6 \times 10^{-6} \text{ m} = 6 \times 10^{-4} \text{ cm}$$

1-4 解: 
$$\Delta y = \frac{r_0}{d} \lambda = \frac{50}{0.02} \times 5000 \times 10^{-8} = 0.125 \text{ cm}$$

$$I = A^2 \quad \because I_1 = 2I_2 \quad \therefore A_1 = \sqrt{2}A_2$$

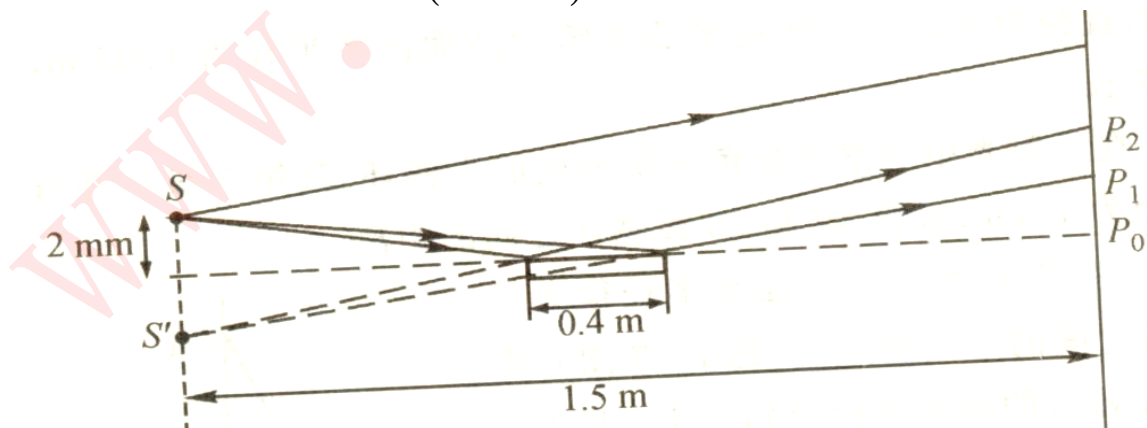
$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} = \frac{2\left(\frac{A_1}{A_2}\right)}{1 + \left(\frac{A_1}{A_2}\right)^2} = \frac{2\sqrt{2}}{1+2} = \frac{2}{3}\sqrt{2} \approx 0.943$$

$$\text{or: } V = \frac{2\sqrt{I_1 I_2}}{I_1 + I_2} = \frac{2\sqrt{2}}{1+2} = \frac{2}{3}\sqrt{2}$$

1-5 解: 
$$\therefore \Delta y = \frac{r+l}{2r \sin \theta} \lambda$$

$$\therefore \sin \theta = \frac{r+l}{2r\Delta y} \lambda = \frac{20+180}{2 \times 20 \times 0.1} \times 7000 \times 10^{-8} = 0.0035$$

$$\theta = \sin^{-1}(0.0035) \approx 0.2^\circ = 12'$$



1-6

解

(1)

$$\Delta y = \frac{r_0}{d} \lambda = \frac{1500}{2 \times 2} \times 500 \times 10^{-7} = 0.1875 \text{ mm} \approx 0.19 \text{ mm}$$

[利用  $\Delta\varphi = \frac{2\pi}{\lambda}\delta = j \cdot 2\pi$ ,  $\delta = \frac{d}{r_0}y - \frac{\lambda}{2}$  亦可导出同样结果。]

(2) 图

$$\therefore \overline{p_0 p_1} = B \tan \theta_1 = B \cdot \frac{a}{A+C} = \frac{0.55 \times 2}{0.55 + 0.4} = \frac{1.1}{0.95} \approx 1.16 \text{ (mm)}$$

$$\overline{p_0 p_2} = (C+B) \tan \theta_2 = (C+B) \cdot \frac{a}{A} = \frac{(0.55 + 0.4) \times 2}{0.55} \approx 3.45 \text{ (mm)}$$

$$\therefore \overline{p_1 p_2} = \Delta l = \overline{p_0 p_2} - \overline{p_0 p_1} = 3.45 - 1.16 = 2.29 \text{ (mm)}$$

$$\Delta N = \frac{\Delta l}{\Delta y} = \frac{2.29}{0.19} \approx 12 \text{ (条)}$$

即：离屏中央 1.16mm 的上方的 2.29mm 范围内，可见 12 条暗纹。（亮纹之间夹的是暗纹）

1-7. 解：  $\therefore 2h\sqrt{n_2^2 - n_1^2 \sin^2 i_1} = (2j+1)\frac{\lambda}{2}$  二级  $j = 0, 1$ ,

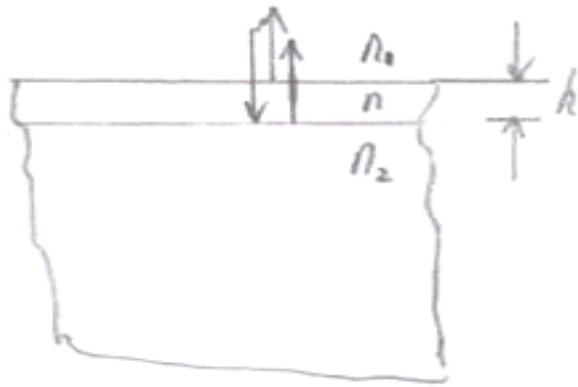
$$\therefore h = \frac{2j+1}{\sqrt{n_2^2 - n_1^2 \sin^2 i_1}} \frac{\lambda}{4}$$

$$= \frac{2 \times 1 + 1}{\sqrt{1.33^2 - 1^2 \times \sin^2 30^\circ}} \times \frac{700}{4} \approx 4260 \text{ \AA}$$

$$\text{or: } \delta = 2h\sqrt{n_2^2 - n_1^2 \sin^2 i_1} + \frac{\lambda}{2}$$

$$2h\sqrt{n_2^2 - n_1^2 \sin^2 i_1} = (2j-1)\frac{\lambda}{2}$$

$$h = \frac{2j-1}{\sqrt{n_2^2 - n_1^2 \sin^2 i_1}} \frac{\lambda}{4} \quad \text{取 } j = 2, \text{ 合题意}$$

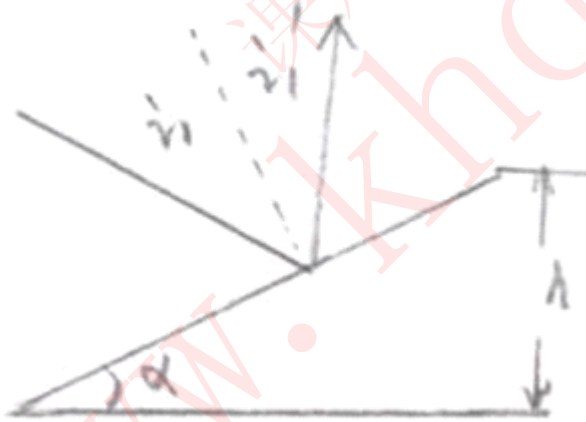


1-8.解:  $\because 2d_0 n_0 \cos i_2 = (2j+1) \frac{\lambda}{2}$

$$i_2 = 0 \quad j = 0$$

$$\text{or: } 2h\sqrt{n_0^2 - n_1^2 \sin^2 i_1} = (2j+1) \frac{\lambda}{2}, \quad i_1 = 0$$

$$\therefore d_{0\min} = \frac{\lambda}{4n} = \frac{5500 \times 10^{-7}}{4 \times 1.38} \approx 10^{-5} \text{ cm}$$



1-9.解: 薄膜干涉中, 每一条级的宽度所对应的空气劈的厚度的变化量为:

$$\begin{aligned} \Delta h = h_{j+1} - h_j &= \left[ (j+1) + \frac{1}{2} \right] \frac{\lambda}{2\sqrt{n_2^2 - n_1^2 \sin^2 i_1}} - \left( j + \frac{1}{2} \right) \frac{\lambda}{2\sqrt{n_2^2 - n_1^2 \sin^2 i_1}} \\ &= \frac{\lambda}{2\sqrt{n_2^2 - n_1^2 \sin^2 i_1}} \end{aligned}$$

若认为薄膜玻璃片的厚度可以略去不计的情况下,

$n_1 = n_2 = 1$ , 又因  $i_1 = i_1' = 60^\circ$ , 则

$$\Delta h = \frac{\lambda}{2\sqrt{1 - \left(\frac{\sqrt{3}}{2}\right)^2}} = \lambda$$

则可认为

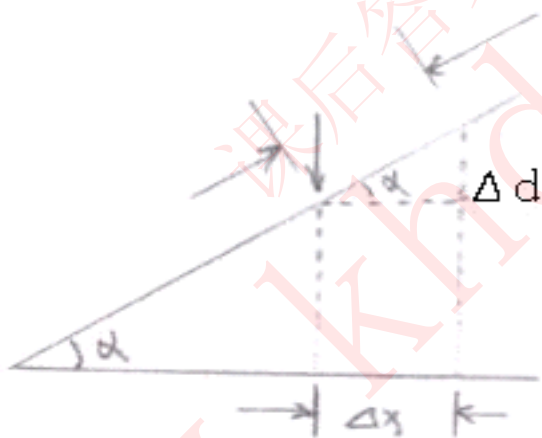
$$\text{Or: } \Delta h = \frac{\lambda}{2 \cos i_2} = \frac{\lambda}{2 \cos 60^\circ} = \lambda$$

而厚度  $h$  所对应的斜面上包含的条纹数为:

$$N = \frac{h}{\Delta h} = \frac{0.05}{5000 \times 10^{-7}} = 100 \text{ (条)}$$

故玻璃片上单位长度的条纹数为:

$$N' = \frac{N}{l} = \frac{100}{10} = 10 \text{ 条/cm}$$



1-10. 解:  $\because$  对于空气劈, 当光垂直照射时,

$$\text{有 } d_0 = \left(j + \frac{1}{2}\right) \frac{\lambda}{2}$$

$$\therefore \Delta d_0 = d_{02} - d_{01} = \frac{\lambda}{2}$$

$$\text{又} \because \Delta d \approx \alpha \cdot \Delta x \approx \alpha \cdot \Delta l$$

$$\text{而 } \alpha \approx \frac{d_0}{l}$$

$$\therefore \frac{d_0 \cdot \Delta l}{l} = \frac{\lambda}{2}$$

$$\begin{aligned} \lambda &= \frac{2d_0 \cdot \Delta l}{l} = \frac{2 \times 0.036 \times 1.4}{179} \\ &= 5.631 \times 10^{-4} \text{ (mm)} = 563.1 \text{ nm} \end{aligned}$$

1-11. 解:  $\because$  是正射,  $i_1 = 0$ ,

$$\therefore \delta = 2n_2d_0 - \frac{\lambda}{2} = j\lambda \quad \text{相长(最强)}$$

$$\therefore 2n_2d_0 = (2j+1)\frac{\lambda}{2}$$

$$\lambda = \frac{4n_2d_0}{2j+1} = \frac{4 \times 1.5 \times 1.2 \times 10^{-6}}{2j+1}$$

$$= \frac{72000 \text{ \AA}}{2j+1}$$

$$\text{or: } 400 \text{ nm} \leq \frac{7200 \text{ nm}}{2j+1} \leq 760 \text{ nm}$$

$$1 \leq \frac{18}{2j+1} \leq 1.9$$

$$\therefore j = 5, 6, 7, 8$$

$$\text{若用 } \delta = 2n_2d_0 + \frac{\lambda}{2} = j\lambda$$

$$\text{则 } j = 6, 7, 8, 9$$

当  $j=1$  时,  $\lambda_1=2400nm$

当  $j=2$  时,  $\lambda_2=1440nm$

当  $j=3$  时,  $\lambda_3=1028nm$

当  $j=4$  时,  $\lambda_4=800nm$

当  $j=5$  时,  $\lambda_5=654.5nm$

当  $j=6$  时,  $\lambda_6=553.8nm$

当  $j=7$  时,  $\lambda_7=480nm$

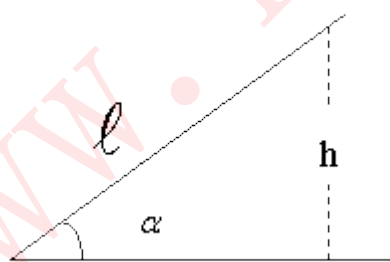
当  $j=8$  时,  $\lambda_8=423.5nm$

当  $j=9$  时,  $\lambda_9=378.9nm$

可见, 在  $400nm \rightarrow 760nm$  中心有  $654.5nm$ 、  
 $553.8nm$ 、 $480nm$ 、 $423.5nm$ 。

1-12. 解:  $\because \Delta h = N \cdot \frac{\lambda}{2}$

$$\therefore \lambda = \frac{2\Delta h}{N} = \frac{2 \times 0.25 \times 10^6}{909} \approx 5500 \text{ \AA} = 550 \text{ nm}$$



1-13 . 解 :

$$\because \Delta d_0 = \frac{\lambda}{2} \approx \alpha \Delta \chi = \alpha \Delta l$$

$$\Delta \ell = \frac{\ell}{N}$$

$$\text{即: } \frac{\lambda}{2} = \alpha \cdot \frac{\ell}{N}$$

$$\Delta d_0 = N \cdot \frac{\lambda}{2}$$

$$\Delta d_0 = \alpha \cdot \ell$$

$$\therefore \alpha = \frac{N\lambda}{2\ell}$$

$$\therefore \alpha = \frac{\lambda}{2\Delta \ell} = \frac{\lambda N}{2\ell}$$
$$= \frac{5890 \times 10^{-8} \times 20}{2 \times 4}$$

$$= 1.4725 \times 10^{-4} \text{ (rad)}$$

$$= 0.00844^\circ$$

$$= 30.384'$$

$$= 30.4''$$

取两棱镜之间的夹角为  $\beta = 90^\circ - \alpha = 89^\circ 59' 29.6''$

1-14. 解: (1) 
$$\Delta h = N \cdot \frac{\lambda}{2} = 1000 \times \frac{5000 \times 10^{-7}}{2} = 0.25 \text{ mm}$$

$$(2) \because 2nh \cos \theta_j = \begin{cases} j\lambda \\ (j + \frac{1}{2})\lambda \end{cases}$$

中心亮斑的级别由下式决定:  $(\cos \theta_j = 1)$

$$2nh = j_0 \lambda$$

所以, 第  $j$  个亮环的角半径  $\theta_j$  满足



$$\cos\theta_j = \frac{(j_0 - j)\lambda}{2nh} = 1 - \frac{j\lambda}{2nh};$$

第 $j$ 个暗环的角半径 $\theta_j$ 满足

$$\cos\theta_j = \frac{[j_0 - (j - \frac{1}{2})]\lambda}{2nh} = 1 - \frac{(j - \frac{1}{2})\lambda}{2nh}.$$

[若中心是暗斑, 则第 $j$ 个暗斑的角半径 $\theta_j$ ]

$$\text{满足 } \cos\theta_j = 1 - \frac{(j + \frac{1}{2})\lambda}{2nh}$$

于是: 第1级暗环的角半径 $\theta$ 为

(对于第1级暗环, 每部分 $j=0$ 时亮斑)

$$\cos\theta = 1 - \frac{\lambda}{4nh} = 1 - \frac{\lambda}{4\Delta h} \quad (\text{此处 } n=1, h = \Delta h \text{ 移动距离})$$

$$= 1 - \frac{5000 \times 10^{-7}}{4 \times 0.25}$$

$$= 1 - 5 \times 10^{-7}$$

$$= 0.9995$$

$$\therefore \theta = 1.8^\circ$$

$$\text{or: (2) 解: } 2h \cos\theta_j = \begin{cases} j\lambda \\ (j + \frac{1}{2})\lambda \end{cases}$$

中心亮斑对应于  $\theta_j = 0$  处, 即  $2h = j\lambda$  (1)

对第一暗环而言, 立有  $2h \cos \theta_j = (2j+1) \frac{\lambda}{2}$  (2)

$$\text{由(1) - (2): } 2h(1 - \cos \theta_j) = -\frac{\lambda}{2} \quad 1 - \cos \theta_j = -\frac{\lambda}{4h}$$

$\because \theta_j$  很小, 将  $\cos \theta_j$  展开为:  $\cos \theta_j = 1 - \frac{\theta_j^2}{2!} + \frac{\theta_j^4}{4!} \dots$

略去高次项, 有:  $1 - (1 - \frac{\theta_j^2}{2!}) = -\frac{\lambda}{4h}$

$$\text{即: } \theta_j^2 = \frac{\lambda}{2h} \quad (\text{这里应取 + 号})$$

$$\theta_j = \sqrt{\frac{\lambda}{2h}} = \sqrt{\frac{500 \times 10^{-7}}{2 \times 0.25}} = \sqrt{10 \times 10^{-4}}$$

$$= 3.2 \times 10^{-2} = 0.032 \text{ (rad)} = 1.8^\circ$$

$$\therefore 2h \cos \theta_j = \begin{cases} j\lambda & \text{相长 亮} \\ (j - \frac{1}{2})\lambda & \text{相消 暗} \end{cases}$$

(2) 解之:

依题意（同上）有：

$$\begin{cases} 2h = j\lambda & (1) \\ 2h\cos\theta_j = (j - \frac{1}{2})\lambda & (2) \end{cases}$$

$$(1) - (2): 2h(1 - \cos\theta_j) = \frac{\lambda}{2}, \quad 1 - \cos\theta_j = \frac{\lambda}{4h}.$$

$$\begin{aligned} \because \theta_j \text{ 很小, } \theta_j \approx \sin\theta_j \quad \therefore \cos\theta_j &= \sqrt{1 - \sin^2\theta_j} = [1 - \theta_j^2]^{\frac{1}{2}} \\ &= 1 - \frac{1}{2}\theta_j^2 + \frac{1}{4}\theta_j^4 \dots \end{aligned}$$

略去高次项，有：

$$1 - \cos\theta_j = 1 - (1 - \theta_j^2)^{\frac{1}{2}} \approx 1 - (1 - \frac{1}{2}\theta_j^2) = \frac{\theta_j^2}{2} = \frac{\lambda}{4h} \quad \text{即: } \theta_j^2 = \frac{\lambda}{2h}$$

$$\therefore \theta_j = \sqrt{\frac{\lambda}{2h}} = \dots = 1.8^\circ.$$

1-15

解

$$\because r_* = \sqrt{(2j+1)\frac{\lambda}{2}R} \quad \text{即: } r_*^2 = (2j+1)\frac{\lambda}{2}R$$

$$\text{亦即: } r_1^2 = (2j+1)\frac{\lambda}{2}R, \quad r_2^2 = [2(j+5)+1]\frac{\lambda}{2}R$$

$$\text{于是: } r_2^2 + r_1^2 = \frac{10}{2}\lambda R = 5\lambda R$$

$$\therefore \lambda = \frac{r_2^2 - r_1^2}{5R} = \frac{D_2^2 - D_1^2}{20R}$$

$$= \frac{(4.6 \times 10^{-3})^2 - (3 \times 10^{-3})^2}{20 \times 1.03}$$

$$= 0.5903 \times 10^{-6} \quad (m) \quad 8$$

$$= 590.3 \quad nm$$

$$\because r_{\text{亮}} = \sqrt{(2j-1)\frac{\lambda}{2}R} \quad j=1, 2, 3, \dots$$

1-16. 解:

$$\text{即: } \begin{cases} r_3 = \sqrt{\frac{5}{2}\lambda R} & r_{20} = \sqrt{\frac{39}{2}\lambda R} \\ r_2 = \sqrt{\frac{3}{2}\lambda R} & r_{19} = \sqrt{\frac{37}{2}\lambda R} \end{cases}$$

$$\text{而: } r_3 - r_2 = \sqrt{\frac{5}{2}\lambda R} - \sqrt{\frac{3}{2}\lambda R} = 1 \quad (\text{mm})$$

即:

$$\frac{5}{2}\lambda R + \frac{3}{2}\lambda R - 2\sqrt{\frac{5}{2}\lambda R} \cdot \sqrt{\frac{3}{2}\lambda R} = 1$$

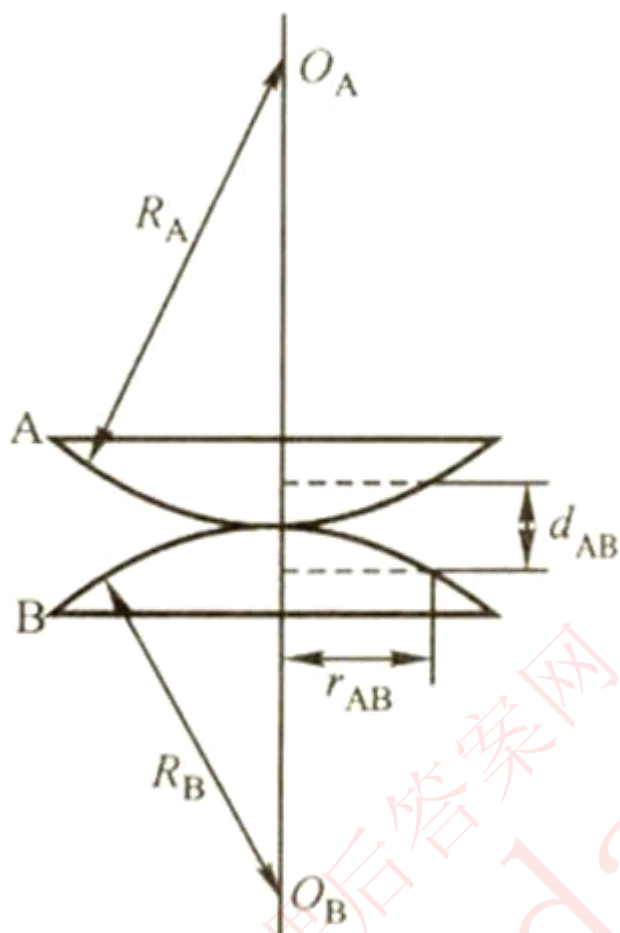
$$4\lambda R - \sqrt{15}\lambda R = 1$$

$$\therefore \lambda R = \frac{1}{4 - \sqrt{15}} \approx 7.873$$

而

$$\begin{aligned} r_{20} - r_{19} &= \sqrt{\frac{39}{2}\lambda R} - \sqrt{\frac{37}{2}\lambda R} \\ &= \sqrt{\frac{39}{2} \times 7.873} - \sqrt{\frac{37}{2} \times 7.873} \\ &= 0.322 \quad (\text{mm}) \end{aligned}$$

$$\therefore \Delta r = r_{20} - r_{19} \approx 0.322 \text{ mm} \quad (= 0.039\text{cm})$$



1-17. 解:  $\because h = \frac{r^2}{2R}$

$$\therefore h_{AB} = h_A + h_B = \frac{r_{AB}^2}{2R_A} + \frac{r_{AB}^2}{2R_B}$$

$$= \frac{r_{AB}^2}{2} \left( \frac{1}{R_A} + \frac{1}{R_B} \right)$$

同理:  $h_{BC} = \frac{r_{BC}^2}{2} \left( \frac{1}{R_B} + \frac{1}{R_C} \right)$

$$h_{AC} = \frac{r_{AC}^2}{2} \left( \frac{1}{R_A} + \frac{1}{R_C} \right)$$

又  $\because$  对于暗环来说, 有

$$\delta = 2h - \frac{\lambda}{2} = (2j+1)\frac{\lambda}{2},$$

$$\text{即: } h = j\lambda/2$$

∴ 对于A、B组合, 第10个暗环有

$$10\lambda = r_{AB}^2 \left( \frac{1}{R_A} + \frac{1}{R_B} \right)$$

$$\text{同样: } 10\lambda = r_{BC}^2 \left( \frac{1}{R_A} + \frac{1}{R_B} \right)$$

$$10\lambda = r_{AC}^2 \left( \frac{1}{R_A} + \frac{1}{R_C} \right)$$

$$\text{于是: } \frac{1}{R_A} + \frac{1}{R_B} = \frac{10\lambda}{r_{AB}^2} \quad (1)$$

$$\frac{1}{R_B} + \frac{1}{R_C} = \frac{10\lambda}{r_{BC}^2} \quad (2)$$

$$\frac{1}{R_A} + \frac{1}{R_C} = \frac{10\lambda}{r_{AC}^2} \quad (3)$$

由(1)-(2)+(3) 得:

$$\begin{aligned} \frac{2}{R_A} &= 10\lambda \left( \frac{1}{r_{AB}^2} - \frac{1}{r_{BC}^2} + \frac{1}{r_{AC}^2} \right) \\ \text{即: } \frac{2}{R_A} &= 5\lambda \left( \frac{1}{r_{AB}^2} - \frac{1}{r_{BC}^2} + \frac{1}{r_{AC}^2} \right) \\ &= 5 \times 6000 \times 10^{-10} \left[ \frac{1}{(4 \times 10^{-3})^2} - \frac{1}{(4.5 \times 10^{-3})^2} + \frac{1}{(5 \times 10^{-3})^2} \right] \\ &\doteq 3 \times 0.0531 = 0.15935 \quad (m^{-1}) \end{aligned} \quad (4)$$

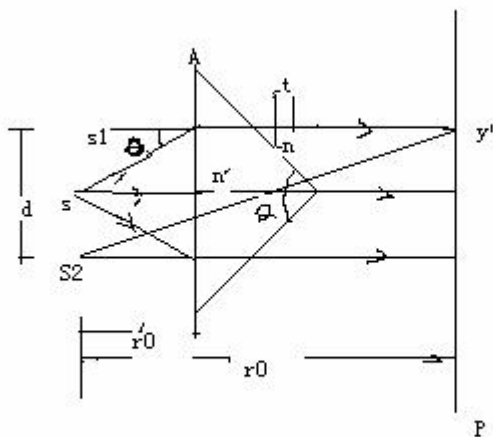
$$\therefore R_A = 6.275 \doteq 6.28 \quad (m)$$

$$\begin{aligned} \text{(4)代入(1): } \frac{1}{R_B} &= \frac{10\lambda}{r_{AB}^2} - \frac{1}{R_A} \\ &= \frac{10 \times 6000 \times 10^{-10}}{(4 \times 10^{-3})^2} - 0.15935 = 0.21565 \quad (m^{-1}) \end{aligned}$$

$$\therefore R_B = 4.637 \doteq 4.64 \quad (m)$$

$$\begin{aligned} \text{(4)代入(3): } \frac{1}{R_C} &= \frac{10\lambda}{r_{AC}^2} - \frac{1}{R_A} \\ &= \frac{10 \times 6000 \times 10^{-10}}{(5 \times 10^{-3})^2} - 0.15935 = 0.08065 \quad (m^{-1}) \end{aligned}$$

$$\therefore R_C = 12.399 \doteq 12.4 \quad (m)$$



的性质相当于虚光源

$S_1, S_2$  由近似条件  $\theta \approx (n-1)A$  和几何关系:  $\theta = \tan \theta = d/2r^2$  得:  $d = 2r^2(n-1)A$  而  $2A + \alpha = \pi$

所以:  $A = (\pi - \alpha)/2 = (180^\circ - 179^\circ 32') = 14' = 14 \times \pi / (60 \times 180)$  (rad)

又因为: 为插入肥皂膜前, 相长干涉的条件为:

$$d y / r_0 = i \lambda$$

插入肥皂膜后, 相长干涉的条件为:

$$d y' / r_0 - (n-1)t = i \lambda$$

所以:  $d(y' - y) / r_0 - (n-1)t = 0$

$$t = d(y' - y) / (n-1) r_0 = 2 r_0 (n-1) A (y' - y) / (n-1) r_0$$

$$= 2 \times 5 \times (1.5 - 1) \times 14 \times 0.08 \pi / (60 \times 180) (1.35 - 1) (5 + 95)$$

$$\text{故: } = 4.65 \times 10^{-5} (cm) = 4.65 \times 10^{-7} m$$

1-19, (1) 图 (b) 中的透镜由 A, B 两部分胶合而成, 这两部分的主轴都不在该光学系统的中心轴线上, A 部分的主轴  $OA F_A$  在系统中心线下 0.5cm 处, B 部分的主轴  $OB F_B$  则在中心线上方 0.5cm 处,  $F_A, F_B$  分别为 A, B 部分透镜的焦点。由于单色点光源 P 经凸透镜 A 和 B 后所成的像是对称的, 故仅需考虑 P 经 B 的成像位置  $P_B$  即可。

$$\text{所以: } 1/s' - 1/s = 1/f', \text{ 所以: } 1/s' = 1/f' + 1/s = 1/50 + 1/-25 = -1/50$$

$$\text{所以: } s' = -50(cm)$$

$$\text{又因为: } \beta \equiv y'/y = s'/s, \text{ 所以: } y' = s'y/s = 2 \times 0.5 = 1.0(cm)$$

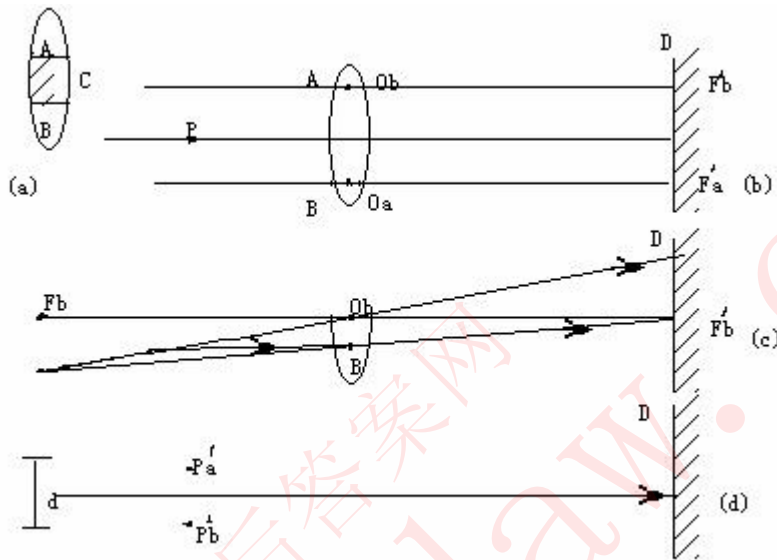
故所成的虚像  $P_B$  在透镜 Bd 的主轴下方 1cm 处, 也就是在光学系统的对称轴下方 0.5cm

处。同理，单色点光源 P 经透镜 A 所成的虚像  $P_A$  在光学系统对称轴上方 0.5cm 处，其光路图仅绘出点光源 P 经凸透镜 B 的成像，此时，虚像  $P_A$  和  $P_B$  就构成想干光源。它们之间的距离为 1cm，

所以：想干光源  $P_A, P_B$  发出的光束在屏上形成干涉条纹，其相邻条纹的间距为：

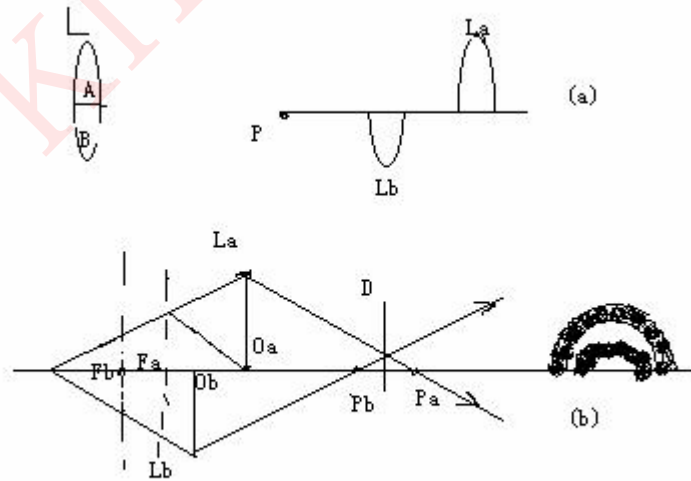
$$\Delta y = r_0 \lambda / d = 100 \times 692 \times 10^{-3} \text{ (cm)}$$

(2) 光屏上呈现的干涉条纹是一簇双曲线。 1-19 题图：



1-20, 解, (1)

如图 (a) 所示，对透镜 L 的下半部分  $L_B$ ，其光心仍在  $O_b$ ，故成像位置  $P_B$  不变，即  $S_1 = 10\text{cm}$  但对透镜上半部分  $L_A$ ，其光心不在  $O_b$ ，而移到  $O_A$ ，则成像位置将在  $P_A$  处，像距



$s_2' = s_2 f / (s_2 + f) = -12.5 \times 5 / (-12.5 + 5) = 25 / 3 = 8.33 \text{ (cm)}$  这样，两个半透镜  $L_A, L_B$ ，所成的实像  $P_A$  和  $P_B$  位于主轴上相距 0.83cm 的两点，光束在  $P_A$  和  $P_B$  之间的区域交叠。



(2) 由于实像  $P_A$  和  $P_B$  购车国内一对想干光源，两想干光束的交叠区域限制在  $P_A$  和  $P_B$  之间，依题意，光屏 D 至于离透镜  $L_B 10.5\text{cm}$  处，恰好在  $P_A$  和  $P_B$  之间，故可以观察到干涉条纹，其条级为半圆形。根据光程差和相位差的关系可以进一步计算出条级的间距。

1-21. 解，(1) 因为:在反射光中观察牛顿环的亮条纹，

$$\delta = 2h - \lambda/2 = i\lambda, \dots, (r_j = \sqrt{(2j+1)R\lambda/2} = \sqrt{2hR})$$

及干涉级  $j$  随着厚度  $h$  的增加而增大，即随着薄膜厚度的增加，任意一个指定的  $j$  级条纹将缩小其半径，所以各条纹逐渐收缩而在中心处消失，膜厚  $h$  增加就相当于金属 的长度在缩短。

所以，但到牛顿环条纹移向中央时，表明 C 的长度在减少。

(2) 因为:  $\Delta h = N\lambda/2 = (\Delta j)\lambda/2$

$$\Delta h = 10 \times 632.8 \div 2 = 3164(\text{nm})$$

所以,  $= 3.164 \times 10^{-3} \text{mm}$

2-1. 解:  $R = \sqrt{k\lambda r_0}$  详见书 P 102~103

$$\begin{aligned} \rho_1 &= \sqrt{1 \times 4500 \times 10^{-10} \times 1} = 6.7 \times 10^{-4}(\text{m}) \\ &= 0.67(\text{mm}) \qquad = 0.067(\text{cm}) \end{aligned}$$

2-2. 解:

$$\begin{aligned} (1) \quad R_1 &= \sqrt{k\lambda r_0} \\ &= \sqrt{k \cdot 5000 \times 10^{-10} \times 4} \\ &= \sqrt{2k} \times 10^{-3}(\text{m}) \\ &= 1.414\sqrt{k} \text{ mm} \\ &= 0.1414\sqrt{k} \text{ cm} \end{aligned}$$

$k$  为奇数时，P 点总得极大值，

$k$  为偶数时，P 点总得极小值。

书 P103 倒 12~11 行

$$(2) \quad d_1 = 2\rho_1 = 0.2828(\text{cm})$$

2-3. 解:

$$\therefore k = \frac{\rho_k^2}{\lambda} \left( \frac{1}{r_0} + \frac{1}{R} \right)$$

$$\therefore k_1 = \frac{(0.5 \times 10^{-3})^2}{5000 \times 10^{-10}} \left( \frac{1}{1} + \frac{1}{1} \right) = 1$$

$$k_2 = \frac{(1 \times 10^{-3})^2}{5000 \times 10^{-10}} \left( \frac{1}{1} + \frac{1}{1} \right) = 4$$

即：实际上仅露出 3 个带

$$\text{即： } A = \frac{1}{2}(a_1 + a_3) \approx a_1$$

$$\text{而 } A_\infty = \frac{a_1}{2}$$

$$\therefore \frac{I}{I_0} = \frac{A^2}{A_\infty^2} = \frac{a_1^2}{(a_1/2)^2} = 4$$

2-4. 解：

$$(1) \because \rho_k = \sqrt{k\lambda r_0}$$

$$\therefore k = \rho_k^2 / \lambda r_0 = \frac{\left( \frac{2.76}{2} \times 10^{-3} \right)^2}{6328 \times 10^{-10} \times 1} \approx 3$$

$\because k=3$  为奇数， $\therefore$  中央为亮点。

(2) 欲使其与 (1) 相反，即为暗点， $K$  为偶数

$$\because r_0 = \rho_k^2 / k\lambda$$

$$\therefore r_0' = \frac{\rho_k^2}{(k-1)\lambda} = \frac{\left( \frac{2.76}{2} \times 10^{-3} \right)^2}{(3-1) \times 6328 \times 10^{-10}} = \frac{3}{2} = 1.5$$

$$\Delta r_1 = r_0' - r_0 = 1.5 - 1.0 = 0.5(m)$$

$\because \Delta r_1 > 0$ ， $\therefore$  向后移动。

$$\text{又 } \because r_0'' = \frac{\rho_k^2}{(k+1)\lambda} = \frac{\left( \frac{2.76}{2} \times 10^{-3} \right)^2}{(3+1) \times 6328 \times 10^{-10}} = \frac{3}{4} = 0.75$$

$$\therefore \Delta r_2 = r_0'' - r_0 = 0.75 - 1.0 = -0.25(m)$$

$\therefore \Delta r_2 < 0$ ,  $\therefore$  向前移动。

故: 应向前移动 0.25m, 或向后移动 0.25m

2-5. 解: (1)  $\because r_1 : r_2 : r_3 : r_4 = 1 : \sqrt{2} : \sqrt{3} : \sqrt{4}$

$$r_0 = 1(m), \quad \lambda = 5000 \text{ \AA}$$

$$r = \sqrt{k\lambda r_0}$$

$$r_1 : r_2 : r_3 : r_4 = \sqrt{k_1} : \sqrt{k_2} : \sqrt{k_3} : \sqrt{k_4}$$

$$\therefore k_1 = 1, \quad k_2 = 2, \quad k_3 = 3, \quad k_4 = 4,$$

$$r_1 = \sqrt{1 \times 5000 \times 10^{-10} \times 1} = 0.707(mm)$$

(2) 由题意知, 该屏对于所参考的点只让偶数半波带透光, 故:

$$A = \sum_k a_{2k} = a_2 + a_4 \approx 2a_2$$

$$\text{而 } A_\infty = \frac{a_2}{2}$$

$$\therefore I = A^2 = 4a_2^2 = 16A_\infty^2 = 16I_0$$

$$\therefore f = r_0 = \frac{\rho_k^2}{k\lambda} = 1(m) \text{ —— 主焦点}$$

(3)

它还有次焦点:  $\pm f/3, \pm f/5,$   
 $\pm f/7 \dots\dots$

故, 光强极大值出现在轴上

$1/3, 1/5, 1/7, \dots\dots 1/(2k+1)$ 等处

$\therefore$  此即将所有偶数半波带挡住了,

而只有所有奇数的半波带透过

2-6. 解:

∴ 在考察点的振幅为

$$A_k = \frac{1}{2}(a_1 + a_{199}) \approx a_1$$

$$\text{即: } I_0 = A_k^2 = a_1^2$$

当换上同样焦距的口径的透镜时,

$$A_{\mu} = A_{\omega} = \frac{a_1}{2} \quad \left( f = r_0' = \frac{\rho_k^2}{k\lambda} \right)$$

$$\text{即: } I = A_f^2 = a_1^2/4$$

$$\therefore \frac{I}{I_0} = \frac{a_1^2/4}{a_1^2} = \frac{1}{4}$$

$$\therefore A = a_1 + a_3 + a_5 + \dots + a_{199} \approx 100a_1$$

$$I = A^2 = 10^4 a_1^2$$

当移去波带片使用透镜后, 透镜对所有光波的相位延迟一样, 所以  $a_1, a_2, a_3, \dots, a_{200}$  的方向是一致的, 即:

$$A_0 = a_1 + a_2 + a_3 + \dots + a_{200} \approx 200a_1$$

$$I_0 = A_0^2 = 4 \times 10^4 a_1^2$$

$$\therefore \frac{I}{I_0} = \frac{10^4 a_1^2}{4 \times 10^4 a_1^2} = \frac{1}{4}$$

2-7.

解

$$\therefore \Delta\varphi = \frac{2\pi}{\lambda} \delta = \frac{2\pi}{\lambda} b \sin \theta \approx \frac{2\pi}{\lambda} b \operatorname{tg} \theta = \frac{2\pi}{\lambda} b \frac{y}{f}$$

$$\therefore y = \frac{\lambda}{2\pi} \cdot \frac{f}{b} \cdot \Delta\varphi$$

$$\begin{aligned} y_1 &= \frac{\lambda}{2\pi} \cdot \frac{f}{b} \cdot \Delta\varphi_1 \\ &= \frac{4800 \times 10^{-7} \times 600}{2\pi \times 0.4} \cdot \frac{\pi}{2} \\ &= 0.18(\text{mm}) \\ &= 0.018(\text{cm}) \end{aligned}$$

$$\begin{aligned} y_2 &= \frac{\lambda}{2\pi} \cdot \frac{f}{b} \cdot \Delta\varphi_2 \\ &= \frac{4800 \times 10^{-7} \times 600}{2\pi \times 0.4} \cdot \frac{\pi}{6} \\ &= 0.06(\text{mm}) \\ &= 0.006(\text{cm}) \end{aligned}$$

2-8. 解:

$\therefore$  次最大值公式:

$$\sin \theta_{20} = \pm 2.46 \frac{\lambda}{b} \approx \frac{5}{2} \frac{\lambda}{b}$$

$$\sin \theta_{30} = \pm 3.47 \frac{\lambda}{b} \approx \frac{7}{2} \frac{\lambda}{b}$$

$$\therefore \pm \frac{7}{2} \frac{\lambda_1}{b} = \pm \frac{5}{2} \frac{\lambda_2}{b}$$

$$\therefore \lambda_1 = \frac{5}{7} \lambda_2 = \frac{5}{7} \times 6000 \approx 4286 \text{ \AA}$$

$$\text{或: } \lambda_1 = \frac{2.46}{3.47} \times 6000 \approx 4254 \text{ \AA}$$

2-9. 解:

$$(1) \quad \therefore \sin \theta_k = k \frac{\lambda}{b}$$

$$y = \operatorname{tg} \theta_1 \cdot f$$

$$\operatorname{tg} \theta_1 \approx \sin \theta_1$$

$$\therefore y = k \frac{\lambda}{b} f$$

$$\therefore y_1 = \operatorname{tg} \theta_1 \cdot f = \sin \theta_1 \cdot f = 1 \times \frac{\lambda}{b} f$$

$$= \frac{5461 \times 10^{-7}}{1} \times 100$$

$$= 0.05461(\text{cm})$$

$$\approx 0.055(\text{cm})$$

$$(2) \quad \therefore \sin \theta_{10} = \pm 1.43 \frac{\lambda}{b} \approx \pm \frac{3 \lambda}{2 b}$$

$$y = \operatorname{tg} \theta \cdot f, \operatorname{tg} \theta \approx \sin \theta$$

$$\therefore y_{10} = 1.43 \frac{\lambda}{b} f$$

$$= 1.43 \times \frac{5461 \times 10^{-7}}{1} \times 100$$

$$\approx 0.078(\text{cm})$$

$$\text{or: } = \frac{3}{2} \cdot \frac{\lambda}{b} f$$

$$= \frac{3}{2} \times \frac{5461 \times 10^{-7}}{1} \times 100$$

$$\approx 0.082(\text{cm})$$

$$(3) \quad \therefore \sin \theta_k = k \frac{\lambda}{b}, \quad k = 3, \quad y = k \frac{\lambda}{b} f$$

$$\begin{aligned}
 \therefore y_3 &= \operatorname{tg} \theta_3 \cdot f' \approx \sin \theta_3 \cdot f' \\
 &= 3 \times \frac{\lambda}{b} f' \\
 &= 3 \times \frac{5461 \times 10^{-7}}{1} \times 100 \\
 &\approx 0.164(\text{cm})
 \end{aligned}$$

2-10. 解:

$$(1) \quad \because \sin \theta_k = k \frac{\lambda}{b}$$

$$y = \operatorname{tg} \theta \cdot f'$$

$$\operatorname{tg} \theta \approx \sin \theta$$

$$Y = k \lambda f' / b$$

$$\begin{aligned}
 \text{即: } \Delta y &= y_2 - y_1 = (\operatorname{tg} \theta_2 - \operatorname{tg} \theta_1) \cdot f' \\
 &= (\sin \theta_2 - \sin \theta_1) \cdot f' \\
 &= \left( 2 \times \frac{\lambda}{b} - 1 \times \frac{\lambda}{b} \right) \cdot f' \\
 &= \frac{\lambda}{b} f'
 \end{aligned}$$

$$\begin{aligned}
 \therefore \lambda &= \frac{b}{f'} \times (y_2 - y_1) = \frac{0.2 \times 0.885}{300} \\
 &= 5.9 \times 10^{-4}(\text{mm}) = 5900 \text{ \AA}
 \end{aligned}$$

$$\begin{aligned}
 (2) \quad \Delta y' &= y_2' - y_1' = \frac{\lambda'}{b} f' = \frac{1 \times 10^{-7}}{0.2} \times 300 \\
 &= 1.5 \times 10^{-4}(\text{cm})
 \end{aligned}$$

2-11. 解:

$\because N = 3$ , 缝宽为  $b$ , 相邻缝间不透明

的距离  $a = d = 3b$

光栅常数  $d' = a + b = 4b$

∴ 最小值有  $N - 1 = 3 - 1 = 2$  个

次最大有  $N - 2 = 3 - 2 = 1$  个

缺级级次为

$$j = k \frac{d'}{b} = 4k = \pm 4, \pm 8, \pm 12, \dots$$

$$\text{又} \because A_j = \frac{A_0 N}{\pi j} \times \frac{d'}{b} \times \sin \left( j\pi \times \frac{d'}{b} \right)$$

$$\frac{I_j}{I_0} = \frac{A_j^2}{(A_0 N)^2} = \left( \frac{4}{\pi j} \right)^2 \sin^2 \left( j \frac{\pi}{4} \right)$$

$$\approx \frac{1.6}{j^2} \sin^2 \left( j \frac{\pi}{4} \right)$$

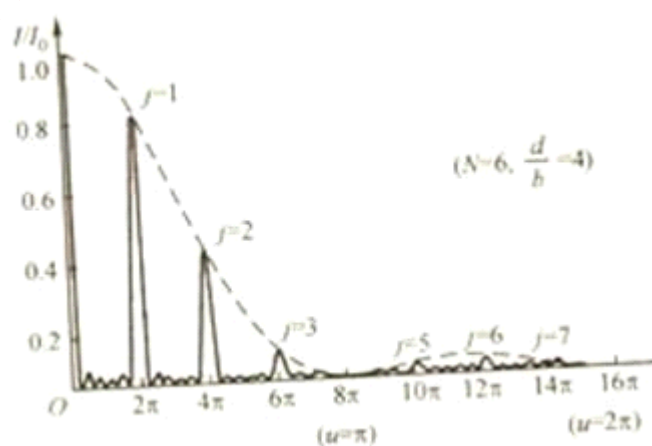
$$\therefore \frac{I_1}{I_0} \approx 0.80$$

$$\frac{I_2}{I_0} = 0.40$$

$$\frac{I_3}{I_0} = 0.09$$

$$\frac{I_4}{I_0} = 0$$

$$\frac{I_5}{I_0} = 0.03$$





$$\frac{I_6}{I_0} = 0.04$$

$$\frac{I_7}{I_0} = 0.02$$

$$\frac{I_8}{I_0} = 0$$

其大致图形如上所示（仅画出正值）

2-12. 解:  $\because d \sin \theta = j\lambda$

$$\therefore \sin \theta = \frac{j\lambda}{d} \quad \left( d = \frac{1}{N} \right)$$

$$\therefore \sin \theta_1 = \frac{j_1 \lambda_1}{d} = 50 \times 1 \times 7600 \times 10^{-7} = 0.038$$

$$\theta_1 \approx 2.18^\circ$$

$$\sin \theta_2 = \frac{j_2 \lambda_2}{d} = 50 \times 2 \times 4000 \times 10^{-7} = 0.04$$

$$\theta_2 \approx 2.29^\circ$$

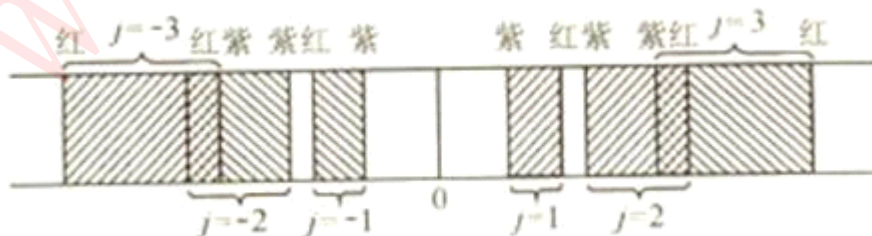
$$\Delta \theta = \theta_2 - \theta_1$$

$$= 2.29^\circ - 2.18^\circ$$

$$= 0.11^\circ$$

$$\approx 6.7'$$

$$\approx 7'$$



2-13. 解:  $\because d \sin \theta = j\lambda$  即  $\sin \theta = \frac{j\lambda}{d}$

$$\text{对 } j=1, \quad \sin \theta_1 = \frac{\lambda_{\text{短}}}{d} = \frac{7600 \text{ \AA}}{d}$$

$$j=2, \quad \sin \theta_2 = 2 \frac{\lambda_{\text{长}}}{d} = \frac{8000 \text{ \AA}}{d}$$

由于  $\theta_2 > \theta_1$ , 故第一级和第二级不会重叠

$$\text{而 } j=2, \quad \sin \theta_2 = 2 \frac{\lambda_{\text{短}}}{d} = \frac{15200 \text{ \AA}}{d}$$

$$j=3, \quad \sin \theta_3 = 3 \frac{\lambda_{\text{长}}}{d} = \frac{12000 \text{ \AA}}{d}$$

由于  $\theta_3 < \theta_2$ , 故第二级和第三级可以重叠。

其重叠范围计算如下:

$$\text{对重叠部分, 有: } j_2 \lambda_1 = j_3 \lambda_2$$

$$\text{即: } 2\lambda_1 = 3\lambda_2$$

$$2 \times (4000 \sim 7600) = 3 \times (4000 \sim 7600)$$

$$8000 \sim 15200 = 12000 \sim 22800$$

可见重叠部分是:

$$12000 \sim 15200 = 12000 \sim 15200$$

其相交的波长是:

$$6000 \sim 7600 \text{ 与 } 4000 \sim 5076$$

$$\text{即: 二级光谱的 } 6000 \sim 7600 \text{ \AA}$$

与三级光谱的  $4000 \sim 5067 \text{ \AA}$  重叠

$$\therefore d \sin \theta = j\lambda, \quad \sin \theta = \frac{j\lambda}{d}$$

2-14. 解:

对中央最大值,  $j = 0, \sin \theta = 0, \theta_0 = 0$

对第二十级主最大,  $\sin \theta_{20} = \frac{j_{20} \lambda}{d}$

$$\therefore \Delta \theta = \theta_{20} - 0 = \sin^{-1} \frac{j_{20} \lambda}{d}$$

$$\text{即: } \frac{j_{20} \lambda}{d} = \sin \Delta \theta$$

$$\begin{aligned} \therefore d &= \frac{j_{20} \lambda}{\sin \Delta \theta} \\ &= \frac{20 \times 5890 \times 10^{-8}}{\sin 15^\circ 10'} \\ &\approx 4.5 \times 10^{-3} (\text{cm}) \end{aligned}$$

$$\text{故: } N = \frac{1}{d} = \frac{1}{4.5 \times 10^{-3}} \approx 222 (\text{条/cm})$$

2-15. 解:  $\therefore d(\sin \theta \pm \sin \theta_0) = j \lambda$

(1) 当垂直入射时,  $\sin \theta_0 = 0$ , 有  $d \sin \theta = j \lambda$

$j$ 取最大值,  $\sin \theta = 1$ , 即  $\theta = \theta_{\max} = 90^\circ$  而  $d = \frac{1}{N}$

$$\begin{aligned} \therefore j_{\max} &= \frac{d}{\lambda} = \frac{1}{\lambda N} = \frac{1}{5980 \times 10^{-7} \times 400} = \frac{1}{0.2356} \\ &= 4.24 \approx 4 (\text{级}) \end{aligned}$$

$$\begin{aligned}
 (2) j_{\max} &= \frac{d(\sin \theta_0 + 1)}{\lambda} \\
 &= \frac{1}{\lambda N} (\sin 30^\circ + 1) \\
 &= 4 \times \left( 1 + \frac{1}{2} \right) \\
 &= 6(\text{级})
 \end{aligned}$$

2-16. 解:  $\because d(\sin \theta + \sin \theta_0) = j\lambda, \sin \theta_0 = 1, d = \frac{1}{N}$

$$\begin{aligned}
 \therefore j\lambda &= d \sin \theta = \frac{\sin \theta}{N} = \frac{\sin 30^\circ}{250} = \frac{1}{2 \times 250} \\
 &= \frac{1}{500} = 0.002(\text{mm}) = 20000 \text{ \AA}
 \end{aligned}$$

故: 当  $j = 2$  时,  $\lambda = 10000 \text{ \AA}$

当  $j = 3$  时,  $\lambda = 6667 \text{ \AA}$

当  $j = 4$  时,  $\lambda = 5000 \text{ \AA}$

当  $j = 5$  时,  $\lambda = 4000 \text{ \AA}$

当  $j = 6$  时,  $\lambda = 333 \text{ \AA}$

$\therefore$  可出现的光有:

$\lambda_1 = 4000 \text{ \AA}$  紫(色)

$\lambda_2 = 5000 \text{ \AA}$  绿(色)

$\lambda_3 = 6667 \text{ \AA}$  红(色)

2-17 . 解 : ( 1 )

$$2\theta = 2 \frac{\lambda}{b} = 2 \times \frac{6240 \times 10^{-7}}{0.012} = 0.104(\text{rad})$$

(2)  $\because d \sin \theta = j\lambda, \sin \theta \approx \theta$

$$\therefore j = \frac{d \cdot \theta}{\lambda} = \frac{0.041 \times (0.104/2)}{6240 \times 10^{-7}} \approx 3.4 = 3 \text{级}$$

或：单缝衍射花样包络下的范围内  
共有光谱级数由下式确定：

$$\frac{d}{b} = \frac{0.041}{0.012} \approx 3.42 = 3 \text{级}$$

即： $j = 0, \pm 1, \pm 2, \pm 3$

$\therefore$  共有7条条纹

(3)

$$\begin{aligned} \Delta\theta &= \frac{\lambda}{Nd \cos\theta} \\ &= \frac{6240 \times 10^{-7}}{10^3 \times 0.041 \times \cos\left(\frac{0.104}{2} \times \frac{180}{\pi}\right)} \\ &= \frac{6240 \times 10^{-7}}{10^3 \times 0.041 \times 0.9986} \\ &\approx 1.524 \times 10^{-5} (\text{rad}) \end{aligned}$$

或： $\because \theta$ 角极小，可令 $\cos\theta = 1$ ，则：

$$\Delta\theta = \frac{\lambda}{Nd} = \frac{6240 \times 10^{-7}}{10^3 \times 0.041} = 1.52 \times 10^{-5} (\text{rad})$$

2-18. 解： (1)

$$\begin{aligned}
 d &= \sqrt[3]{\frac{M}{2N\rho}} \\
 &= \sqrt[3]{\frac{58.5}{2 \times 6.02 \times 10^{23} \times 2.17}} \\
 &= \sqrt[3]{2.239 \times 10^{-23}} \\
 &\approx 2.8185 \times 10^{-8} (\text{cm}) \\
 &\approx 2.819 \text{ \AA}
 \end{aligned}$$

$$\therefore \rho = \frac{M}{V}, V = 2Nd^3$$

$$\therefore d^3 = \frac{M}{2N\rho}, d = \sqrt[3]{\frac{M}{2N\rho}}$$

$$(2) \therefore 2d \sin \alpha_0 = j\lambda$$

$$\begin{aligned}
 \therefore \lambda &= \frac{2d \sin \alpha_0}{j} \\
 &= \frac{2 \times 2.819 \times \sin 1^\circ}{2}
 \end{aligned}$$

$$\approx 0.049 \text{ \AA}$$

$$219. \text{ 解: } \therefore 2d \sin \alpha_0 = j\lambda$$

$$\begin{aligned} \therefore \sin \alpha_0 &= \frac{j\lambda}{2d} \\ &= \frac{2 \times 0.0147 \times 10^{-10}}{2 \times 0.28 \times 10^{-9}} \\ &= 0.00525 \end{aligned}$$

$$\alpha_0 \approx 0.3^\circ = 18'$$

注：若将单位换一下，

$$\text{即：} \lambda = 0.0147 \text{ nm}, d = 0.28 \text{ } \overset{\circ}{\text{A}}$$

$$\text{则：} \sin \alpha_0 = \frac{2 \times 0.0147 \times 10^{-9}}{2 \times 0.28 \times 10^{-10}} = 0.525$$

$$\alpha_0 \approx 31.67^\circ \approx 31^\circ 40'$$

or

$$\alpha_0 \approx \varepsilon \alpha_0 = 0.3^\circ = 18'$$

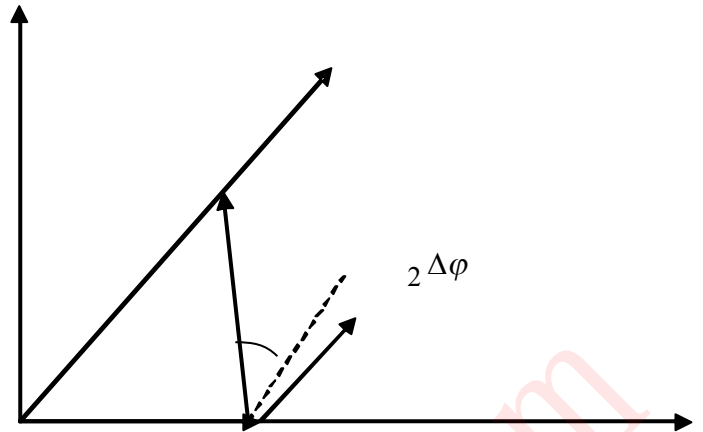
2-20. 证：设单缝衍射的振幅为  $a_\theta$ ，三缝衍射的总振幅为  $A_\theta$ ，则  $A_{\theta x} = a_\theta (1 + \cos \Delta\Phi + \cos \Delta\varphi)$

$$\begin{aligned} A_{\theta y} &= a_\theta (1 + \sin \Delta\Phi + \sin \Delta\varphi), I_\theta = A_\theta^2 = A_{\theta x}^2 + A_{\theta y}^2 \\ &= a_\theta^2 [(1 + \cos \Delta\Phi + \cos \Delta\varphi)^2 + (1 + \sin \Delta\Phi + \sin \Delta\varphi)^2] \\ &= a_\theta^2 [3 + 2(\cos \Delta\Phi + \cos 2\Delta\Phi + \cos 3\Delta\varphi)] \end{aligned}$$

$$\begin{aligned} \text{又} \because a_\theta &= a_0 \frac{\sin u}{u}, \quad u = \frac{\pi b \sin \alpha}{\lambda} \\ \Delta\varphi &= \frac{2\pi d \sin \theta}{\lambda} = 2u, \quad v = \frac{\pi d \sin \theta}{\lambda} \end{aligned}$$

$$\begin{aligned} \therefore I_\theta &= a_0^2 \left( \frac{\sin u}{u} \right)^2 [3 + 2(\cos 2v + \cos 4v + \cos 6v)] \\ &= I_0 \left( \frac{\sin u}{u} \right)^2 [3 + 2(\cos 2v + \cos 4v + \cos 6v)] \end{aligned}$$

其中  $u = \frac{\pi b \sin \alpha}{\lambda}$ ， $v = \frac{\pi d \sin \theta}{\lambda}$ ，得证。



2-21. 解 : ∴ A

$$\approx \mu A \approx \frac{1.0 - 0.5}{20} = 0.025 \text{ (rad)}$$

$$\left( = 0.025 \times \frac{180}{\pi} = 1.433^\circ \right)$$

而单色平行光距劈后的偏向角  $\theta_0 \approx (n-1)A = (1.5-1) \times 0.025 = 0.0125 \text{ (rad)}$

未知劈波前  $d \sin \theta = j \lambda$

当  $j = \pm 1$  时,  $\sum \theta = \pm \frac{\lambda}{d}$

$$\therefore \theta = \sin^{-1} \left( \pm \frac{\lambda}{d} \right) = \sin^{-1} \left( \pm \frac{500 \times 10^{-7}}{2} \times 12000 \right)$$

$$= \sin^{-1} (\pm 0.3) = \pm 17.46^\circ$$

加上劈波后,  $d (\sin \theta' + \sum \theta_0) = \pm \lambda$

$$\text{即: } \sum \theta' = \pm \frac{\lambda}{d} - \sum \theta_0 = \pm \lambda - \sin[(n-1)A]$$

$$\approx \pm \lambda - (n-1)A = \pm 0.3 - 0.0125 = \begin{cases} +0.2875 \\ -0.3125 \end{cases}$$

$$\theta' = \sin \left[ \begin{matrix} +0.2875 \\ -0.3125 \end{matrix} \right] = \begin{cases} +16.17^\circ \\ -18.21^\circ \end{cases}$$

$$\Delta \theta = \theta' - \theta \quad \begin{cases} +16.17^\circ \\ -18.21^\circ \end{cases} \quad \mp \quad 17.46^\circ = -0.75^\circ = -45'$$



2-22. (1) 以题意得:

$$\begin{aligned} \therefore d(\sum \theta + \sum \theta_0) &= j\lambda \quad (\text{同侧}) \\ d(\sum \theta' - \sum \theta) &= j\lambda \quad (\text{异侧}) \\ \therefore 2\sin \theta_0 &= (\sum \theta - \sum \theta_0) \end{aligned}$$

$$\begin{aligned} \sum \theta_0 &= \frac{1}{2} (\sum \theta' - \sum \theta) = \frac{1}{2} (\sin 53^\circ - \sin 11^\circ) \\ &= \frac{1}{2} \times (0.7986 - 0.1908) = 0.3039 \\ \theta_0 &= \sin^{-1} 0.3039 = 17.69^\circ \approx 17.7^\circ \end{aligned}$$

(2)  $\therefore$  当位于法线两侧时:  $d(\sum \theta - \sum \theta_0) = j\lambda$

$$\text{即 } \sum \theta = \sum \theta_0 + j \frac{\lambda}{d}$$

$$\text{对于 } j=1 \text{ 谱线, } \sum 53^\circ = \sum 17.7^\circ + \frac{\lambda}{d}, \quad \frac{\lambda}{d} = \sum 53^\circ - \sum 17.7^\circ$$

$$\text{对于 } j=2 \text{ 谱线, } \sum \theta = \sum \theta_0 + 2 \frac{\lambda}{d} = \sum 17.7^\circ + 2(\sum 53^\circ - \sum 17.7^\circ)$$

$$= 2 \sum 53^\circ - \sum 17.7^\circ = 2 \times 0.7989 - 0.3039 = 1.29 > 1$$

$\therefore$  在法线两侧时, 观察不到第二级谱线

$\therefore$  当位于法线同侧时,  $d(\sum \theta + \sum \theta_0) = j\lambda$

$$j=2 \text{ 时 } \sum \theta = 2 \frac{\lambda}{d} - \sum \theta_0 = 2 \times (\sum 53^\circ - \sum 17.7^\circ)$$

$$= 2 \sum 53^\circ - 3 \sum 17.7^\circ = 2 \times 0.7989 - 3 \times 0.3039 = 0.6861 < 1$$

在法线同侧时, 能观察到第二谱线...

2-23. (1)  $\therefore d \sin \theta = j\lambda$

$$\text{即 } \begin{cases} d \sin \theta_{1=j_1} \lambda \\ d \sin \theta_{2=j_2} \lambda \end{cases}$$

$$d(\sum \theta_2 - \sum \theta_1) = (j_2 - j_1)\lambda = \Delta j \lambda$$

$\therefore$

$$\begin{aligned} d &= \frac{\Delta j \lambda}{\sum \theta_2 - \sum \theta_1} = \frac{1 \times 600}{.0.3 - 0.2} = 6000 (nm) \\ &= 6.0 \times 10^{-3} (mm) \end{aligned}$$

(2)  $\because d = 4b$

$\therefore b = \frac{d}{4} = 1.5 \times 10^{-3} (mm)$

(3)  $\because \sum \theta_m = \sum \frac{\pi}{2}, \quad j_m = \frac{d}{\lambda} = \frac{6000}{600} = 10$

并考虑到  $j = \pm 4, \pm 8$  缺级

$\therefore$  屏上实际呈现的系数级次为

$j = 0, \pm 1, \pm 2, \pm 3, \pm 5, \pm 6, \pm 7, \pm 9。$